

Regular article

Ab initio study on the dynamical properties of the hydrogen abstraction reaction $\text{NH}_2 + \text{OH} \rightarrow \text{NH} + \text{H}_2\text{O}$

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Abstract. The geometry of the transition state of the title reaction was optimized at the unrestricted Hartree–Fock, the spin-unrestricted second-order Møller–Plesset, and the spin-unrestricted quadratic configuration interaction with all single and double substitutions levels of theory. The changes in the geometry, the bound vibrational modes, and the potential energy along the minimum energy path are discussed. Variational transition-state theory rate constants calculated with the tunneling and curvature effect correction agree very well with the experimental values.

Key words: Hydrogen abstraction – Dynamic property – Ab initio MO

1 Introduction

The reactions of the amidogen radical, $\text{NH}_2(X^2B_1)$, with other radicals are important for understanding the thermal De- NO_x process [1], in which NO that is formed during combustion is converted into molecular nitrogen. One of these reactions, $\text{NH}_2 + \text{OH} \rightarrow \text{NH} + \text{H}_2\text{O}$, is considered to be a kinetically sensitive reaction in the thermal De- NO_x process. In 1982, Dean et al. [2] used a rate constant expression, $3.0 \times 10^{10} T^{0.68} \exp(-1200/RT) \text{ cm}^3 \text{ mol}^{-1} \text{ s}^{-1}$, in the mechanism of ammonia oxidation over the temperature range from 1279 to 1323 K. In 1989, Miller and Bowman [1] used another rate constant expression, $4.0 \times 10^6 T^2 \exp(-1000/RT) \text{ cm}^3 \text{ mol}^{-1} \text{ s}^{-1}$, to investigate the thermal De- NO_x mechanism in the temperature range 1150–1350 K. From both the rate constant expressions, we can see that their activation energies are very close, while their rate constants are not consistent with each other. To our knowledge, the dynamical properties of this reaction have not been studied theoretically; therefore, we decided to study this

reaction by using quantum chemistry and chemical reaction dynamics.

Dynamical calculations based on variational transition-state theory (VTST) constitute a practical method for studying polyatomic reactions [3–6]. Such calculations describe a chemical reaction by using ab initio electronic structure information only in the region of configuration space along the reaction path.

In the present paper, we use ab initio molecular orbital theory and the VTST dynamical method for the hydrogen abstraction reaction $\text{NH}_2 + \text{OH} \rightarrow \text{NH} + \text{H}_2\text{O}$. The second section of this paper describes the theoretical methods and computational details. In the third section, the stationary points on the hydrogen abstraction reaction path are optimized, and the minimum energy path (MEP) is calculated along the intrinsic reaction coordinate. The information about the potential energy, geometric variations, and generalized normal mode vibrational frequencies along the reaction path is also discussed. At the end of the third section, the rate constants based on conventional TST and, on VTST are presented and compared with the experimental values.

2 Computational methods

In this work, ab initio molecular orbital calculations were carried out with the GAUSSIAN 92 program [7] for the stationary points on the reaction path of the title reaction. The geometries of the reactants (NH_2 and OH), products (NH and H_2O), and transition states were optimized by using unrestricted Hartree–Fock (UHF) theory [8], spin-unrestricted Møller–Plesset perturbation (UMP) theory [9], and spin-unrestricted quadratic configuration interaction with all single and double substitutions (UQCISD) theory [10], respectively. The Møller–Plesset perturbation (UMP2) calculations include full electron correlation, while in the fourth-order Møller–Plesset perturbation (UMP4) and UQCISD calculations the frozen-core approximation has been employed. Furthermore, we used the scaling all correlation (SAC) method [11] in the UMP4/6-311G** calculation at the UMP2/6-311G** optimized geometries to yield an improved calculation of the barrier height. For the UMP-SAC4//MP2 calculation, the total electronic energy is [11]

$$E_{\text{MP-SAC4//MP2}} = E_{\text{HF}} + (E_{\text{MP4}} - E_{\text{HF}})/f_4,$$

where f_4 is a scaling factor which is assumed to be independent of the geometry for a given system.

The MEP was calculated at the UMP2/6-311G** level of theory using intrinsic reaction coordinate theory [12–14] with a stepsize of 0.02 (amu)^{1/2}bohr. At some points along the intrinsic reaction coordinate, we computed the matrix of force constants and the harmonic vibrational frequencies. Because the shape of the potential-energy curve is an important factor affecting the rate constant, the UMP2 potential profile was refined at the UQCISD(T) and UMP-SAC4 levels with the same basis set.

The canonical VTST rate constant, $k^{\text{CVT}}(T)$, was calculated at a fixed temperature (T) by minimizing the generalized TST rate constant, $k^{\text{GT}}(T, s)$, with respect to the dividing surface at s . The result is expressed as [3–6]

$$k^{\text{CVT}}(T) = \min_s k^{\text{GT}}(T, s) .$$

The generalized TST rate constant, k^{GT} , for temperature T and dividing surface at s is

$$k^{\text{GT}}(T, s) = \frac{\sigma Q^{\text{GT}}(T, s)}{\beta h Q^{\text{R}}(T)} \exp[-\beta V_{\text{MEP}}(s)] .$$

In this equation, s is the location of the generalized transition state on the MEP; σ is the symmetry factor accounting for the possibility of two or more symmetry-related reaction paths; β equals $(k_{\text{B}}T)^{-1}$, where k_{B} is Boltzmann’s constant, h is Planck’s constant; $Q^{\text{R}}(T)$ is the reactant’s partition function per unit volume, excluding symmetry numbers for rotation; $V_{\text{MEP}}(s)$ is the classical energy along the MEP with the overall zero of energy at the reactant; $Q^{\text{GT}}(T, s)$ is the partition function of the generalized transition state at s with the local zero of energy at $V_{\text{MEP}}(s)$ and with all rotational symmetry numbers set to unity. For $s = 0$, this equation yields the conventional TST rate constant (k^{TST}). To include quantal effects for motion along the reaction coordinate, $k^{\text{CVT}}(T)$ is multiplied by a ground-state transmission coefficient, $\kappa^{\text{CVT/G}}(T)$ with the zero-curvature tunneling (ZCT) and small-curvature tunneling (SCT) approximations [5,15], which are denoted as $k^{\text{CVT/ZCT}}(T)$ and $k^{\text{CVT/SCT}}(T)$, respectively. The POLYRATE program [16] was employed for the calculations of the reaction rate constants.

3 Results and discussion

The optimized geometrical parameters and harmonic frequencies of the reactants (NH₂ and OH) and products (NH and H₂O) are listed in Table 1. It can be seen that at the UHF level the bond lengths are slightly shorter and the bond angles are slightly greater than the experimental

ones. When electronic correlation correction is introduced, the optimized geometries agree better with the experimental values. At the UMP2 level the deviations between the calculated and the experimental vibrational frequencies are mostly less than 9%, while at the UHF level the deviations are mostly greater than 9%, except for the OH and NH radicals. This provides confidence in the UMP2 level for studying this reaction process.

The geometric parameters and harmonic frequencies of the transition state optimized at various levels are displayed in Table 2. The transition state is a triplet state and $\langle S^2 \rangle = 2.038$. The imaginary vibrational mode and the atom-numbering system of the transition state are shown in Fig. 1. At the UHF/6-311G** level, the breaking N₍₁₎–H₍₃₎ bond of the transition state is stretched by about 16% compared to that in NH₂, while the forming H₍₃₎–O₍₄₎ bond is still 34% longer than that of H₂O. At the UMP2/6-311G** level, the breaking N₍₁₎–H₍₃₎ bond is stretched by about 7% compared to that in NH₂, and the forming H₍₃₎–O₍₄₎ bond length is 44% longer than that in H₂O. It is obvious that the transition state structure is more reactant-like than productlike. On the other hand, the breaking N₍₁₎–H₍₃₎ bond and the forming H₍₃₎–O₍₄₎ bond of the transition state at the UMP2 level are slightly shorter and longer than those at the UHF level, respectively. Also, the geometric parameters of the transition state optimized at the UQCISD/6-311G** level of theory are almost consistent with those optimized at the UMP2 level of theory. This shows that the geometry of the transition state of this reaction optimized at the UMP2/6-311G** level of theory is quite reliable. Comparing the frequencies at the UMP2 level with those at the UHF level, we find that the imaginary frequency at the former level is about 2100 cm⁻¹ less than that at the latter level, while there are smaller variations in the real frequencies.

In order to illustrate the applicability of an UHF single-configuration reference state, a multiconfiguration self-consistent-field calculation was carried out for the transition state at the UMP2/6-311G** geometry. A complete active space involving six electrons and six orbitals with the 6-311G** basis set was performed. The result shows that the coefficient of the ground-state

Table 1. Optimized geometric parameters (Å and degree) and harmonic frequencies (cm⁻¹) of reactants and products

	NH ₂		OH	NH	H ₂ O		NH ₂			OH	NH	H ₂ O		
	R _{N-H}	θ _{H-N-H}	R _{O-H}	R _{N-H}	R _{O-H}	θ _{H-O-H}	ω(a ₁)	ω(a ₁)	ω(b ₁)	ω(σ)	ω(σ)	ω(a ₁)	ω(a ₁)	ω(b ₁)
UHF/6-31G	1.015	108.5	0.967	1.032	0.950	111.5	1651	3552	3647	3831	3372	1736	3988	4145
UHF/6-31G*	1.013	104.4	0.958	1.024	0.947	105.5	1711	3607	3707	4003	3529	1826	4070	4188
UHF/6-31G**	1.013	104.3	0.955	1.024	0.943	105.9	1656	3609	3706	4056	3514	1770	4145	4262
UHF/6-311G**	1.012	104.1	0.951	1.023	0.941	105.4	1643	3599	3683	4053	3501	1751	4141	4236
UMP2/6-31G*	1.028	103.4	0.979	1.039	0.968	104.0	1632	3423	3545	3740	3366	1735	3778	3920
UMP2/6-31G**	1.023	102.6	0.971	1.035	0.961	103.8	1596	3484	3599	3844	3407	1684	3893	4031
UMP2/6-311G**	1.024	102.1	0.966	1.035	0.957	102.5	1545	3459	3560	3860	3392	1667	3910	4017
UQCISD/6-311G**	1.029	101.8	0.969	1.042	0.957	102.7	1578	3416	3514	3833	3331	1722	3914	4030
Experimental ^a	1.024	103.3	0.971	1.035	0.958	104.5	1497 ^b	3219	3301	3735 ^c	3282 ^c	1588 ^d	3650	3742

^a Ref. [17]

^b Ref. [18]

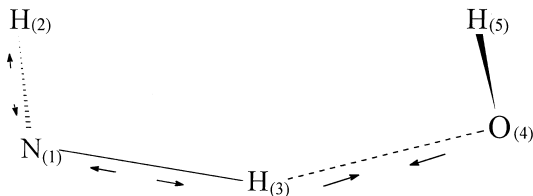
^c Ref. [19]

^d Ref. [20]

Table 2. Optimized geometric parameters and harmonic frequencies of the transition state

	Geometry parameters (Å and degree)								
	R_{12}	R_{13}	R_{34}	R_{45}	θ_{312}	θ_{431}	θ_{543}	φ_{4312}	φ_{5431}
UHF/6-31G	1.023	1.190	1.276	0.964	102.5	174.2	101.2	1.1	178.6
UHF/6-31G*	1.018	1.186	1.259	0.956	100.0	168.9	97.9	48.4	99.0
UHF/6-31G**	1.018	1.174	1.260	0.953	99.9	169.0	97.6	46.1	99.9
UHF/6-311G**	1.016	1.174	1.262	0.949	101.0	162.6	96.2	29.8	80.4
UMP2/6-31G*	1.030	1.111	1.372	0.979	104.0	146.9	99.9	9.3	73.0
UMP2/6-31G**	1.026	1.095	1.384	0.972	103.6	148.0	99.8	9.2	68.2
UMP2/6-311G**	1.027	1.093	1.386	0.967	102.7	150.2	98.5	9.1	67.8
UQCISD/6-311G**	1.031	1.104	1.384	0.968	103.4	149.6	98.4	6.7	69.2

	Frequencies (cm^{-1})								
	ω_1	ω_2	ω_3	ω_4	ω_5	ω_6	ω_7	ω_8	ω_F
UHF/6-31G	3875	3514	1563	1043	740	556	389	48	<i>i</i> 3801
UHF/6-31G*	4022	3612	1546	1161	762	510	424	66	<i>i</i> 3790
UHF/6-31G**	4083	3610	1506	1136	782	522	433	33	<i>i</i> 3722
UHF/6-311G**	4078	3598	1429	1298	797	548	441	77	<i>i</i> 3687
UMP2/6-31G*	3730	3473	1770	1209	1087	693	402	345	<i>i</i> 1949
UMP2/6-31G**	3834	3525	1825	1155	1092	600	371	200	<i>i</i> 1640
UMP2/6-311G**	3847	3492	1777	1144	1056	586	378	192	<i>i</i> 1514

**Fig. 1.** Structure and imaginary vibrational mode of the transition state

configuration is 0.982 and the absolute magnitudes of the coefficients of other configurations are all less than about 0.088. Thus, the single dominant determinant can afford a sufficiently accurate reference of this reaction.

The potential-energy barrier (V^*) and the heat of reaction (ΔH) at each level of theory are listed in Table 3. The absolute values of ΔH at the UMP2 levels are about 9 kcal/mol greater than those at the UHF levels. The heats of reaction obtained by single-point energy calculations at the UMP4, UQCISD(T), and UMP-SAC4 levels based on the UMP2/6-311G** geometries are -25.94 , -25.42 , and -27.34 kcal/mol, respectively. The heat of reaction at the UMP-SAC4 level is in good agreement with the experimental value. From Table 3, we can see that there are significant differences in the potential barrier height for the different basis sets and different levels of calculations. At the UHF level the potential barrier height is apparently overestimated, while at the UMP2 and UQCISD levels it is still much greater than the experimental ones. Accurate theoretical potential energy barriers are calculated at the UMP4, UQCISD(T), and UMP-SAC4 levels at the UMP2/6-311G** geometries. Apparently, the value of the UQCISD(T) barrier is slightly greater than the value of Dean et al. [2], and the value of the UMP-SAC4 barrier is slightly less than that of Miller and Bowman [1].

The MEP was calculated with a step size of 0.02 ($\text{amu}^{1/2}\text{bohr}$) at the UMP2/6-311G** level. Then the

UMP2/6-311G** potential-energy profile was further refined with the UQCISD(T) and UMP-SAC4 levels. The minimum-potential-energy curve, $V_{\text{MEP}}(s)$, and the corresponding vibrationally adiabatic ground-state potential-energy curve, $V_a^G(s)$, based on the UMP-SAC4 method, are shown in Fig. 2. The main geometrical changes along the MEP are shown in Fig. 3. It appears that the $\text{H}_{(3)}\text{--O}_{(4)}$ distance shortens linearly along s and reaches the bond length of H_2O at about $s = 0.8$ ($\text{amu}^{1/2}\text{bohr}$), while the $\text{N}_{(1)}\text{--H}_{(3)}$ bond length starts elongating at about $s = -0.2$ ($\text{amu}^{1/2}\text{bohr}$) and tends linearly to infinity. Both the $\text{N}_{(1)}\text{--H}_{(2)}$ and the $\text{O}_{(4)}\text{--H}_{(5)}$ bond lengths do not vary during the reaction process. It is thus evident that the hydrogen abstraction from $\text{N}_{(1)}$ to $\text{O}_{(4)}$ essentially takes place in the region of $s = -0.2\text{--}0.8$ ($\text{amu}^{1/2}\text{bohr}$).

The frequency changes of the eight bound vibrational modes calculated at the UMP2/6-311G** level are shown in Fig. 4. At the beginning of the reaction, there exists the stretching vibrational mode of OH, which is related to mode 1, and the three vibrational modes of NH_2 , which are related to modes 4, 3, and 2. At the end of the reaction, three vibrational modes of H_2O are associated with modes 5, 3, and 1, and the NH stretching vibration is associated with mode 2. Modes 6, 7, and 8 appear only near the transition state and their frequencies are smaller. The frequency of mode 5 increases significantly as the reaction proceeds and reaches the symmetric bending vibrational frequency of H_2O at about $s = 0.6$ ($\text{amu}^{1/2}\text{bohr}$), while the frequency of mode 4, relating to the symmetric bending vibration of NH_2 , decreases rapidly after the transition state and tends to zero. The frequencies of modes 1 and 2 have no obvious variations during the course of the reaction; however, we can easily find that the change in frequency of mode 3 is the most noticeable one. It starts from the symmetric stretching vibrational frequency of the NH_2 radical, drops rapidly after about $s = -0.5$ ($\text{amu}^{1/2}\text{bohr}$), and reaches the minimum (about 1500 cm^{-1}) at about

Table 3. Potential energy barrier (V^\ddagger) with zero-point vibrational energy correction (ZPE) and heat of reaction (ΔH_{298}^0) in kilocalories per mole

	Forward reaction		Reverse reaction		ΔH_{298}^0
	V_r^\ddagger	$V_r^\ddagger + \Delta ZPE$	V_r^\ddagger	$V_r^\ddagger + \Delta ZPE$	
Optimized					
UHF/6-31G	18.42	16.76	38.52	36.36	-19.32
UHF/6-31G*	21.09	19.78	40.04	37.88	-18.09
UHF/6-31G**	19.92	18.44	40.7	38.28	-19.80
UHF/6-311G**	19.73	18.72	40.69	38.74	-20.02
UMP2/6-31G*	7.48	8.01	34.44	33.52	-26.76
UMP2/6-31G**	5.22	5.48	33.85	33.42	-27.94
UMP2/6-311G**	4.59	4.67	33.91	33.26	-28.51
UQCISD/6-311G**	2.82		28.78		-25.02
Single-point energy calculations at the UMP2/6-311G** geometry					
UMP4/6-311G**	3.65	3.76	30.4	29.78	-25.94
UQCISD(T)/6-311G**	1.43	1.54	27.66	27.04	-25.42
UMP-SAC4	0.69	0.80	28.84	28.22	-27.34
Experimental		1.00 ^a			-28.2 ^c
		1.20 ^b			

^a Ref. [1]

^b Ref. [2]

^c The heat of reaction was obtained from the experimental heats of formation of the reactants (NH₂ and OH) and products (NH and H₂O), which are taken from Ref. [21]

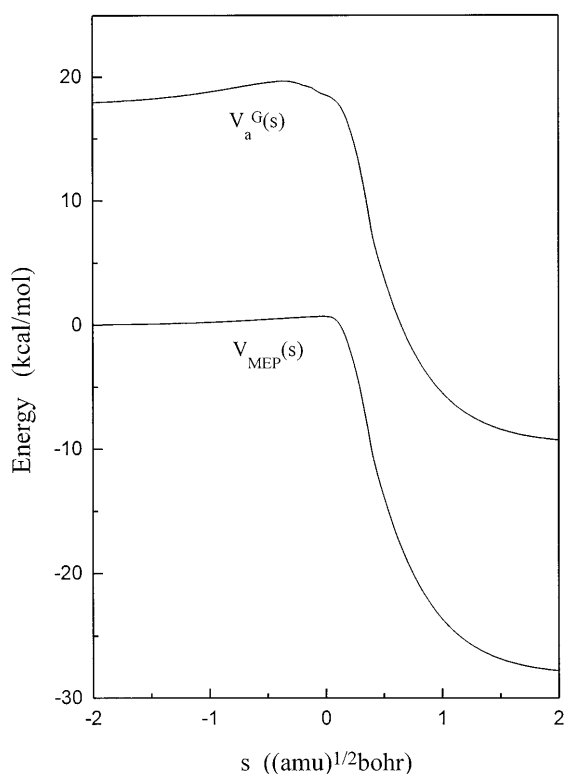


Fig. 2. Minimum energy path, $V_{MEP}(s)$, and vibrationally adiabatic ground-state potential-energy curve, $V_a^G(s)$ at the UMP-SAC4 level of theory

$s = 0.2$ (amu)^{1/2}bohr. Then, at about $s = 0.5$ (amu)^{1/2}bohr it rapidly increases and reaches the symmetric stretching vibrational frequency of H₂O at about $s = 1.0$ (amu)^{1/2}bohr. Namely, mode 3 represents mainly the hydrogen atom abstraction process. In the course of the frequency change of mode 3 there is a minimum of about 1800 cm⁻¹ and the dip occurs over $s = -0.5$ – 0.8 (amu)^{1/2}bohr. This means that the hydrogen abstraction reaction happens substantially in the narrow region from $s = -0.5$ to $s = 0.8$ (amu)^{1/2}bohr.

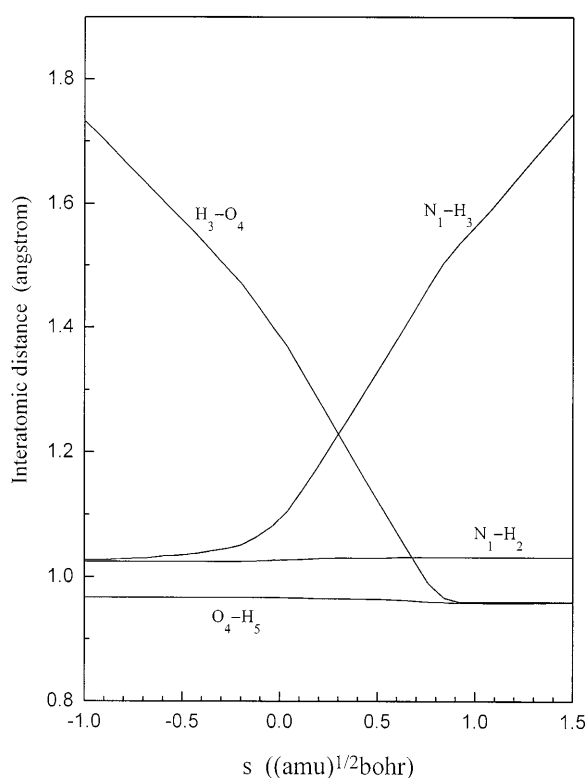


Fig. 3. Changes in interatomic distances calculated at the UMP2/6-311G** level of theory

In this region, the concerted transforming process of the hydrogen atom H₍₃₎ from the stretching vibration of the old bond N₍₁₎–H₍₃₎ to the stretching vibration of the new bond O₍₄₎–H₍₃₎ takes place. This region is approximately the same as where the main change in geometry depicted in Fig. 3 occurs; therefore, mode 3 can be referred to as the “reactive mode” in the hydrogen abstraction reaction. The coupling constants between the MEP and the vibrational modes orthogonal to the MEP show that there is a strong coupling between

the MEP and mode 3 in the reactant side of the transition state. The effective energy exchange between mode 3 and the MEP would favor the hydrogen abstraction reaction of OH from NH₂.

The reaction rate constants for the temperature range from 400 to 3000 K, which are calculated by conventional TST and by VTST with the ZCT and SCT contributions at the UMP2, UQCISD(T), and UMP-SAC4 levels of theory are listed in Table 4. Arrhenius plots of the UMP-SAC4, UMP2, and experimental rate constants are shown in Fig. 5. It is found the reaction rate constants calculated at the UQCISD(T) and UMP-SAC4 levels are in good agreement with the values of Miller and Bowmann over the temperature range 700–3000 K and with the values of Dean et al. over the temperature range 400–800 K, while those at the UMP2 level deviate significantly from the experimental result.

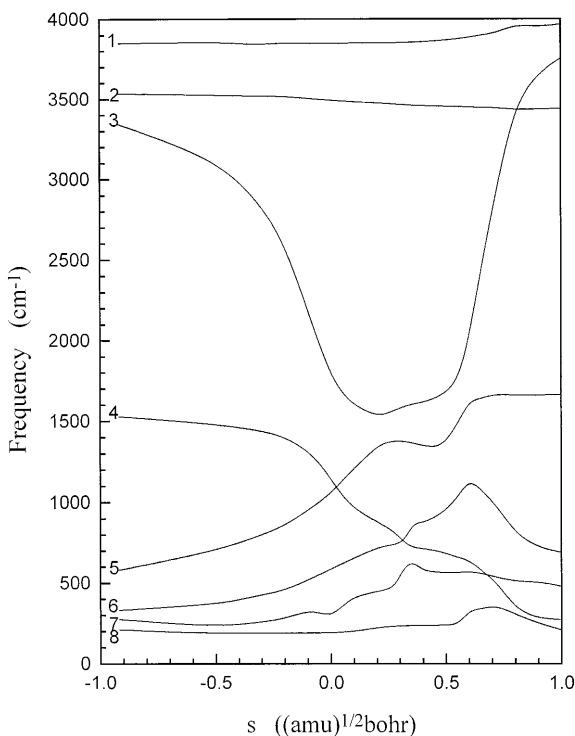


Fig. 4. Changes in vibrational frequencies calculated at the UMP2/6-311G** level of theory

By comparing the results of VTST with conventional TST, one finds that over all the temperature range the variational effect makes the rate constant decrease by about 20%. The locations of the variational transition state are $s = -0.128, -0.111, 0.008,$ and 0.121 (amu)^{1/2}

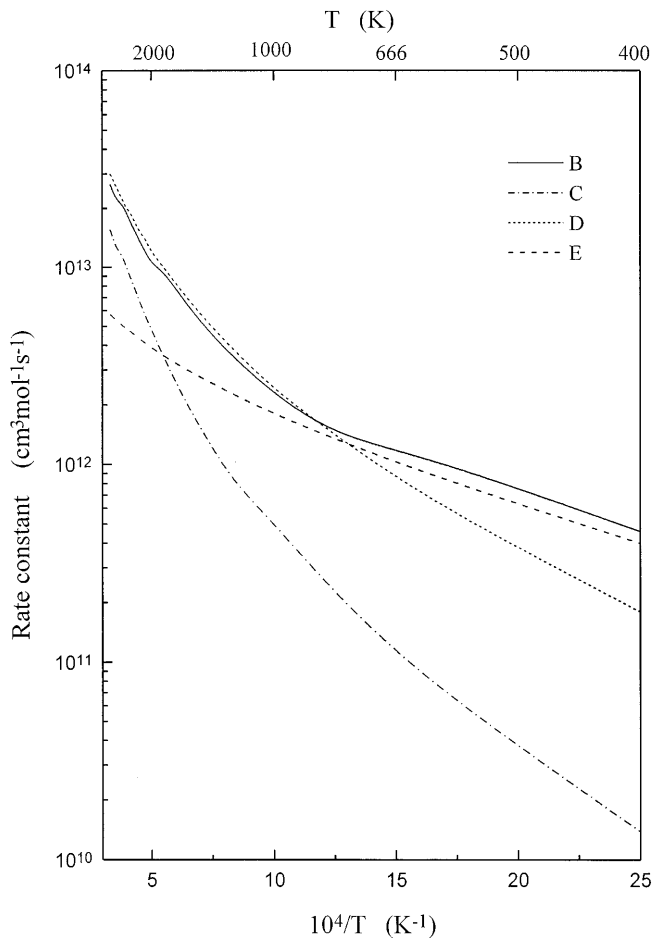


Fig. 5. Arrhenius plot of the theoretical and experimental rate constants versus reciprocal temperature. *B* Canonical variational transition-state theory (CVT)/small-curvature tunneling (SCT) rate constant at UMP-SAC4; *C* CVT/SCT rate constant at UMP2/6-311G**; *D* rate constant expression of Miller and Bowmann [1], $4.0 \times 10^6 T^2 \exp(-1000/RT)$ cm³ mol⁻¹ s⁻¹; *E* rate constant expression of Dean et al. [2], $3.00 \times 10^{10} T^{0.68} \exp(-1200/RT)$ cm³ mol⁻¹ s⁻¹

Table 4. Reaction rate constants (cm³ mol⁻¹ s⁻¹) over the temperature range 400–3000 K

<i>T</i> (K)	UMP2				UQCISD(T)//UMP2				UMP-SAC4//UMP2			
	TST	CVT	CVT/ ZCT	CVT/ SCT	TST	CVT	CVT/ ZCT	CVT/ SCT	TST	CVT	CVT/ ZCT	CVT/ SCT
400	6.18E9	4.03E9	6.36E9	1.39E10	3.30E11	2.15E11	3.39E11	5.13E11	8.29E11	3.05E11	3.78E11	4.60E11
600	5.19E10	4.21E10	5.12E10	7.19E10	7.36E11	5.97E11	7.28E11	8.98E11	1.36E12	8.82E11	9.71E11	1.06E12
1000	4.42E11	4.18E11	4.47E11	5.04E11	2.17E12	2.05E12	2.20E12	2.38E12	3.14E12	2.13E12	2.21E12	2.28E12
1200	8.77E11	7.19E11	7.54E11	8.18E11	3.30E12	2.70E12	2.84E12	3.01E12	4.49E12	3.32E12	3.40E12	3.48E12
1400	1.53E12	1.29E12	1.33E12	1.42E12	4.77E12	4.01E12	4.16E12	4.33E12	6.20E12	4.85E12	4.94E12	5.02E12
1800	3.66E12	3.19E12	3.26E12	3.38E12	8.85E12	7.71E12	7.88E12	8.09E12	1.09E13	9.14E12	9.24E12	9.33E12
2400	9.47E12	8.51E12	8.62E12	8.79E12	1.84E13	1.65E13	1.67E13	1.70E13	2.14E13	1.67E13	1.68E13	1.69E13
3000	1.92E13	1.53E13	1.54E13	1.56E13	3.26E13	2.60E13	2.62E13	2.65E13	3.69E13	2.63E13	2.64E13	2.65E13

bohr at 400, 1000, 2000, and 3000 K, respectively. In addition, Table 4 shows that the tunneling and curvature effects are important at temperatures below 600 K. These quantum effects may be ignored in the investigation of the dynamical properties of this reaction at high temperature.

4 Conclusion

1. The potential-energy barrier calculated at the UMP-SAC4 level of theory is 0.80 kcal/mol and agrees approximately with the experimental one. The heat of reaction at the same theoretical level is -27.3 kcal/mol and is in better agreement with the experimental value.

2. The MEP is followed at the UMP2/6-311G** level by intrinsic reaction coordinate theory. The changes in the geometry along the MEP suggest that the concerted interaction region of both the $N_{(1)}-H_{(3)}$ bond breaking and the $H_{(3)}-O_{(4)}$ bond forming is about $s = -0.2-0.8$ (amu)^{1/2}bohr. The changes in the frequencies and coupling constants along the MEP show that mode 3 plays an important role in the course of the hydrogen abstraction reaction.

3. The VTST rate constants calculated at the UQ-CISD(T) and UMP-SAC4 levels of theory are in good agreement with the values of Miller and Bowman over the temperature range 700–3000 K and with the values of Dean et al. over the temperature range 400–800 K.

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